

# Homework 7

December 2, 2009

1. a. Determine, with explanation, the number of Hamilton cycles in  $K_n$ .  
b. Determine, with explanation, the number of Hamilton cycles in  $K_{n,n}$ .  
c. Determine, with explanation, the number of Euler circuits of  $K_5$ .
2. Show that if  $G$  is a loop-free, connected graph with  $n$  vertices, with more than  $n^2/4$  edges, then  $G$  is not bipartite.
3. Is  $K_{2,3,2}$  planar or not? Justify your answer. Here,  $K_{2,3,2}$  denotes a graph having 12 vertices, and disjoint sets of vertices  $V_1, V_2, V_3$ ,  $|V_1| = |V_3| = 2$ , and  $|V_2| = 3$ , where every vertex in  $V_1$  is connected to every vertex in  $V_2$  by an edge and every vertex in  $V_2$  is connected to every vertex in  $V_3$  by an edge.